



Comprehensive Approach to Student Sectioning

PATAT 2008

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Student Sectioning Problem

- What is Student Sectioning?
 - Student requests courses, system determines classes (sections)
 - Respects course structure, reservations, student preferences, etc.
- Why is Student Sectioning needed?
 - Multi section courses, optimization of student – class enrollments, dynamic reservations of space in sections with excess demand

Primary Course Requests

Add Request

	Type	Course / Free Time		Waitlist	1st Alternative Course	2nd Alternative Course	
1.	Course	ENGL	106	<input checked="" type="checkbox"/>			↓ 🗑
2.	Course	BIOL	110	<input type="checkbox"/>	BIOL 111	BIOL 112	↑ ↓ 🗑
3.	Free Time	3 x 50	MWF 7:30a - 8:20a				↑ ↓ 🗑
4.	Course	COM	114	<input type="checkbox"/>			↑ ↓ 🗑
5.	Course	MA	152	<input type="checkbox"/>	MA 159		↑ ↓ 🗑

Alternative Course Requests

Add Alternative Request

A1.	Course	A&AE	203	<input type="checkbox"/>			↑ ↓ 🗑
A2.	Course	A&D	114	<input type="checkbox"/>	A&D 117		↑ 🗑

Student Sectioning Problem Model

- Variables
 - Individual student course requests
 - including priorities, free times, alternates
- Values
 - A valid set of classes of the requested course (or its alternative), requested free time
- Constraints
 - Course structure, class timetable
 - Course & class limits
 - Course & class reservations
- Solution
 - A set of (most complete) student schedules
 - Maximizing overall request priorities, minimizing use of alternatives, etc.

Primary Course Requests										Add Request
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2. Course	BIOL	110		<input type="checkbox"/>	BIOL 111	BIOL 112				
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1. ENGL 106
 - Lec T 8:30a - 9:20a Full Term HEAV 106
 - Lec (a) F 8:30a - 9:20a Full Term HEAV 106

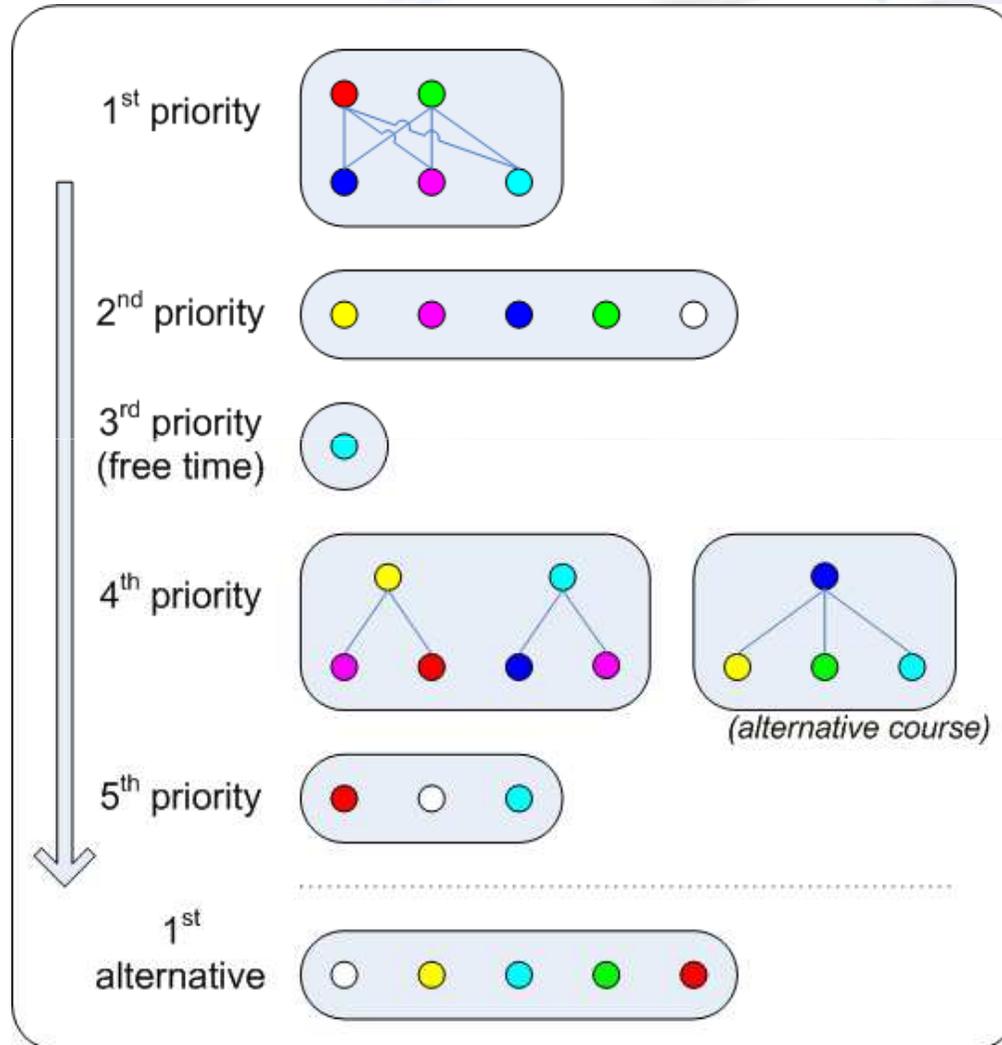
Sel Que Time	Date	Instructor	Require
<input type="radio"/> Th 8:30a - 9:20a	Full Term	T 8:30a	
<input checked="" type="radio"/> F 8:30a - 9:20a	Full Term	W 8:30a	
 - Lec (b) Th 8:30a - 9:20a Full Term ENAD 130

Sel Que Time	Date	Instructor	Ret
<input checked="" type="radio"/> Th 8:30a - 9:20a	Full Term	F 8:	
 - Rec W 8:30a - 9:20a Full Term HEAV 225

Sel Que Time	Date	Instructor
<input type="radio"/> M 8:30a - 9:20a	Full Term	
<input checked="" type="radio"/> W 8:30a - 9:20a	Full Term	
2. BIOL 110
 - Lec TTh 2:30p - 3:20p Full Term LILY 1105 K. Mason
 - Rec T 6:00p - 6:50p Full Term WTHR 360
 - Lab T 3:30p - 5:20p Full Term WTHR 316
 - Pso M 4:30p - 5:20p Full Term LILY G126 K. Mason

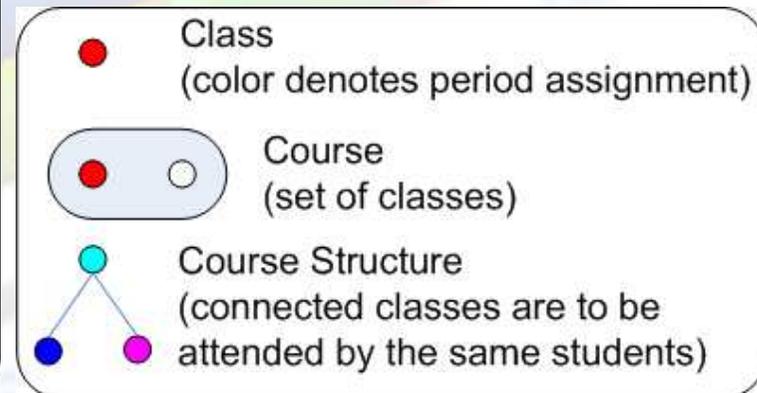
Sel Que Time	Date	Instructor	Requires
<input type="checkbox"/> Arr Hrs		K. Mason	
<input type="radio"/> M 3:30p - 4:20p	Full Term	K. Mason	
<input checked="" type="radio"/> M 4:30p - 5:20p	Full Term	K. Mason	
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3. Free Time MWF 7:30a - 8:20a

Student Sectioning Example

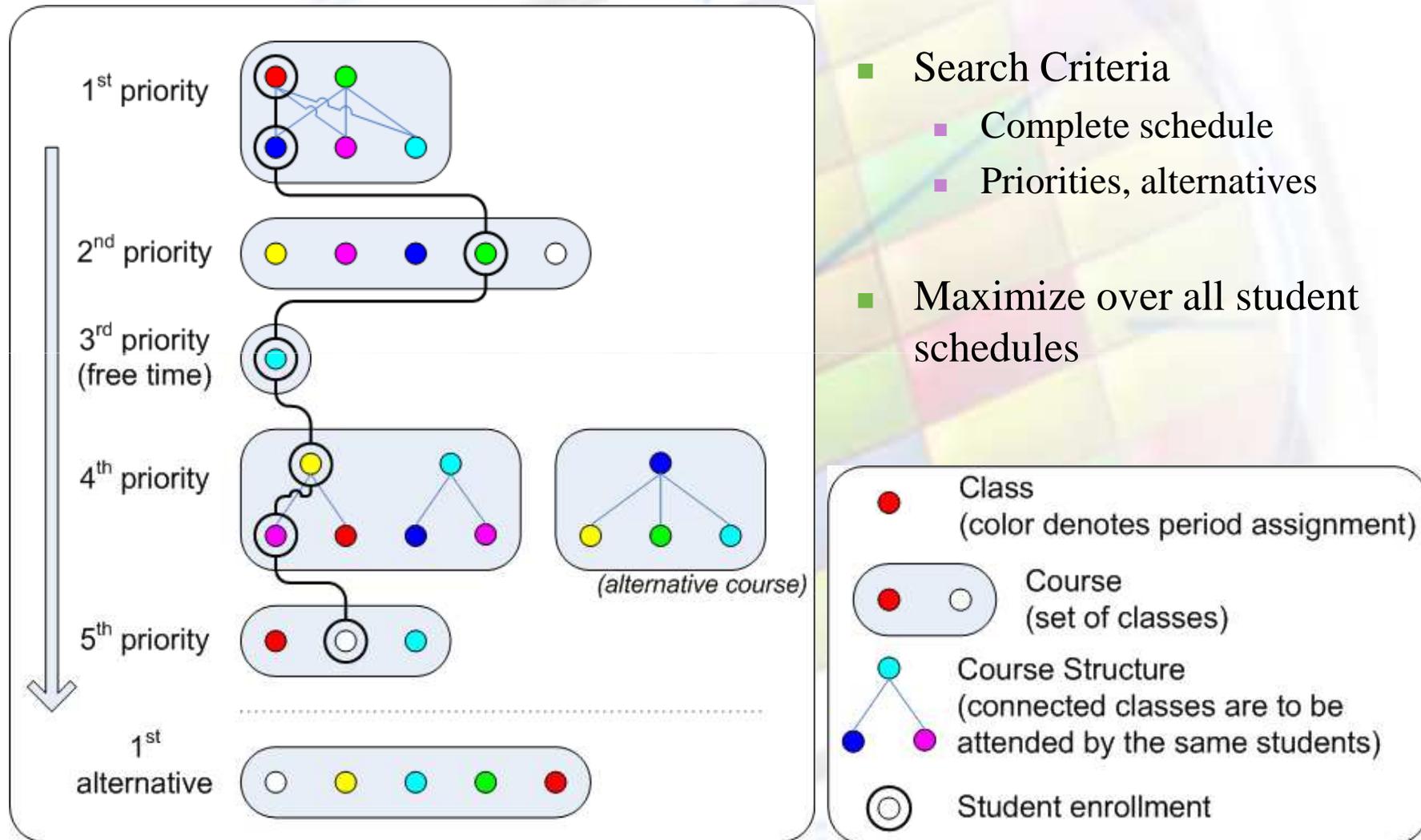


- Input
 - Student requests ordered by priority

- Output
 - Enrollment of a student to valid, not overlapping combinations of classes

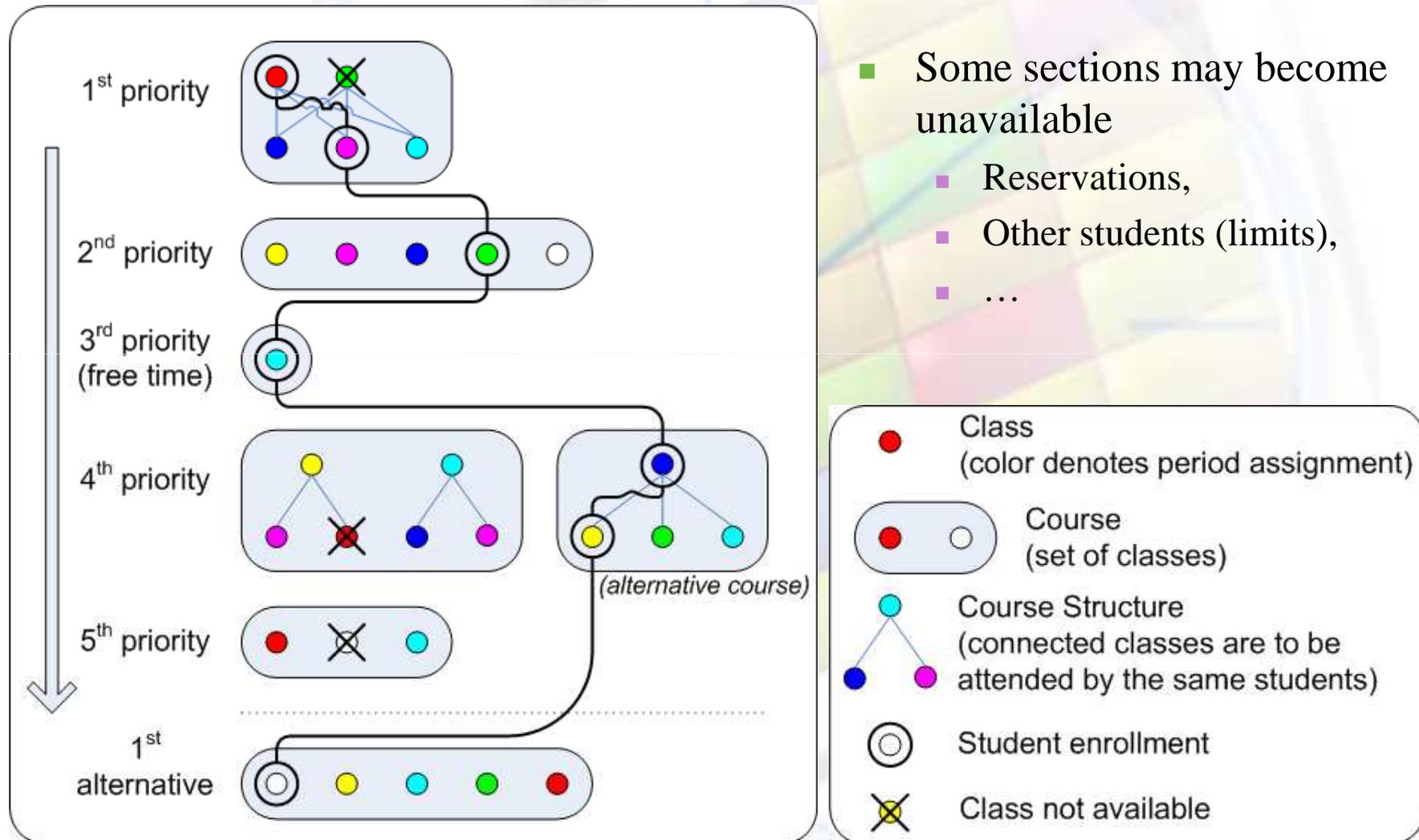


Student Sectioning Example



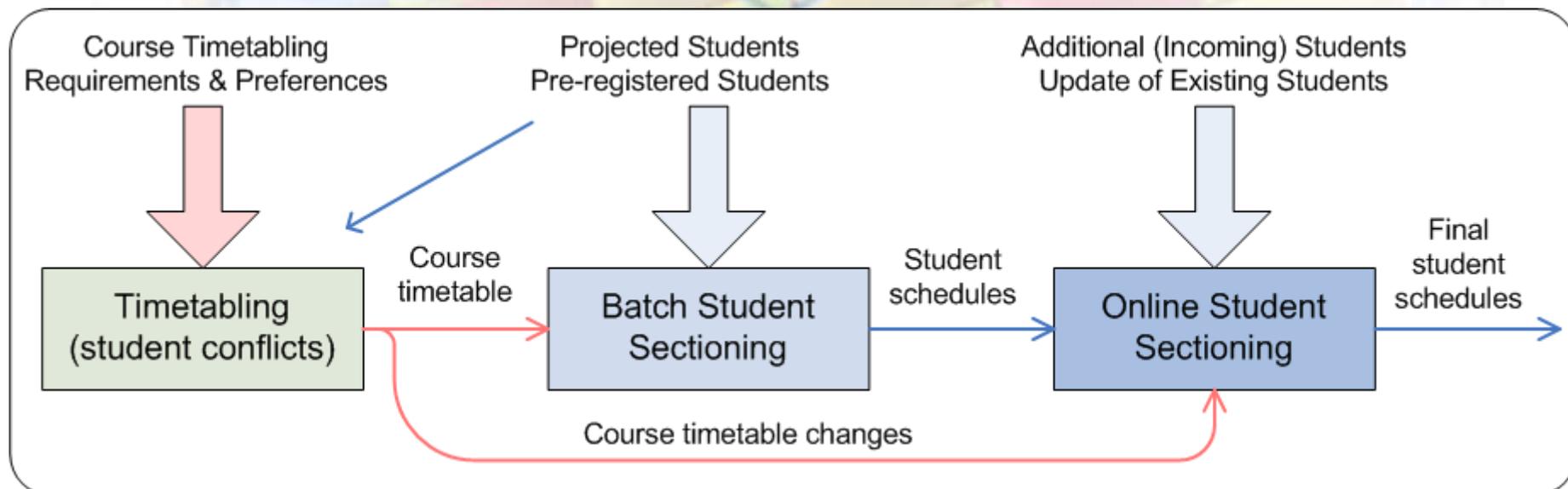
- Search Criteria
 - Complete schedule
 - Priorities, alternatives
- Maximize over all student schedules

Student Sectioning Example



Student Sectioning Phases

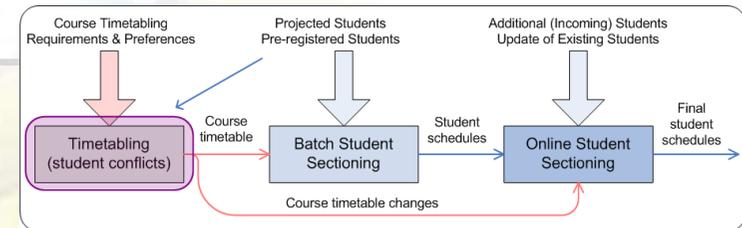
- Initial Sectioning (during timetabling)
 - Timetabling solver minimizes potential student conflicts
- Batch Sectioning
 - Registration of classes for students, reservations, wait lists
- Online Sectioning
 - Registration of first year students, changes in existing enrollments



Initial Sectioning

■ Student Course Requests

- Last-like semester student course demands
- Current course requests from pre-registered students
 - with priorities, alternatives, free times, ...
- Course enrollment projections
- Reservations



Reservations limit what classes/courses are available to which students.

■ → minimization of student conflicts

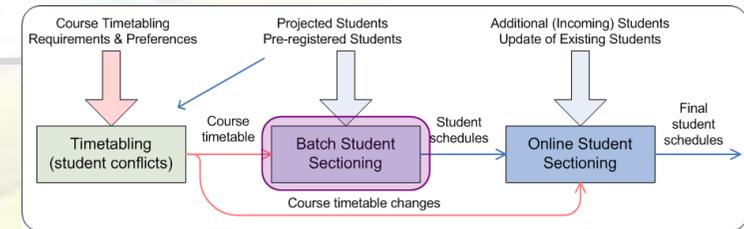
- Two classes overlapping in time (or being back-to-back in distant locations) with common students
- Weighted by request priorities

■ Solver

- Additional criterion in the timetabling solver
- Initial sectioning (before timetabling starts), re-sectioning of students between alternative classes during or after the search

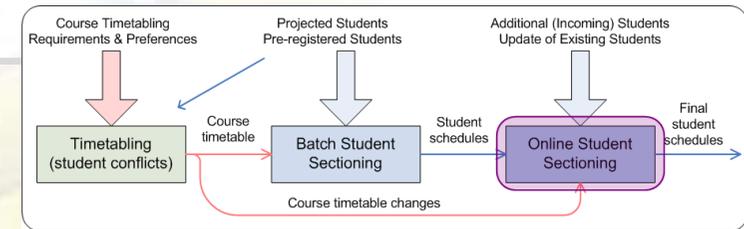
Batch Sectioning

- All students are sectioned altogether
 - Projected student information is used
 - However, first priority is to give pre-registered students full schedule
- → maximization of assigned student requests
 - Pre-registered students are enrolled to classes and/or to wait-lists
 - Reservations for expected (not yet registered) students are created
- Solver
 - CPSolver library is used
 - Open source, local-search based, also used in course timetabling
 - Works with incomplete feasible solutions (no constraint is violated)
 - Various neighborhoods including
 - Branch&bound over all requests of a student
 - Limited-depth backtracking search (over a request and its conflicts)
 - Student swap (swapping of student enrollments between sections)

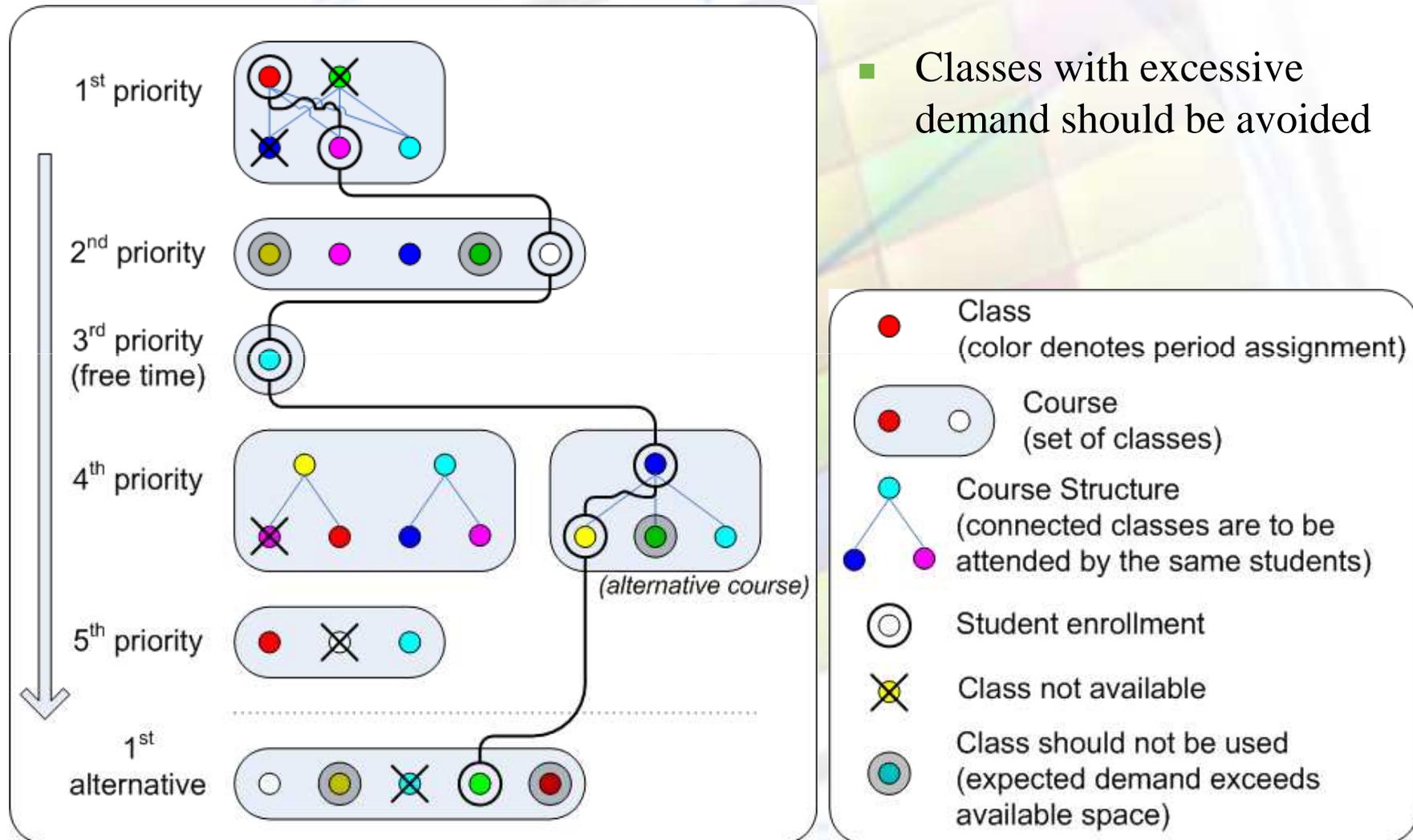


Online Sectioning

- One student is processed at a time
 - Returning a most-complete schedule
 - Considering priorities, alternatives, free-time requests
- → same model (as for batch sectioning), different algorithm
 - Branch&bound returning most complete schedule,
 - optimizing the given preferences (free times, alternatives),
 - avoiding sections reserved for expected students
- Can be an iterative process
 - Student can change requests / choices based on the provided results, assignments are committed at the end
- Reservation of space for expected students
 - Based on projected student enrollments from batch sectioning
 - In each class, a given number of spaces is reserved for new students
 - These reservations are updated as the students are enrolled into classes



Online Student Sectioning Example



- Classes with excessive demand should be avoided

Online Sectioning: Expected / Held Space

- Computation (after batch sectioning)
 - Counter for each class using enrollments of projected (last-like) students
 - Express availability of the class to projected students

$$f_{\text{exp}}(\text{class } c \text{ of a course } C) = \sum_{\substack{\text{projected students } s \\ \text{requesting course } C}} \frac{|\text{available enrollments to } C \text{ containing } c|}{|\text{available enrollments to } C|}$$

- New Student
 - Difference between expected and currently available space
 - Directing students from classes most likely to be needed to other future students
 - Counters are updated after each new student is sectioned
- Existing Student (*students already enrolled in the course*)
 - Held space in a class (unavailable to existing students)
 - Computed as the number of projected students after batch sectioning

Practical Results

- Fall 2007 course timetable from Purdue University
 - 9 000 classes, 570 rooms, 39 000 students with 190 000 course requests
- Student data
 - Last-like (Fall 2006) student course requests
 - 185 494 course requests from 38 740 students
 - Real (Fall 2007, data as of July 11, 2007) student course requests
 - 187 847 course requests from 36 117 students
 - No alternatives, free time requests, or reservations ☹
 - Invalid course requests were eliminated (~2000 requests)
- Test cases
 - Batch sectioning of last-like student course requests
 - → results used for expected / held spaces for online sectioning
 - Batch sectioning of real student course requests
 - Online sectioning of last-like and real student course requests
 - Students are sectioned one by one in a random (or given) order
 - Sectioning by student preferences (uniform, mid-day, early/late)
 - Number of choices provided to the students

Practical Results: Batch versus Online

- Fall 2007 course timetable, Fall 2006/2007 student course requests
- Average and RMS values from 20 independent runs
- Percentage (and actual number) of unassigned course requests
- For online sectioning runs, expected space computed from the best last-like sectioning batch run (316 unassigned course requests)

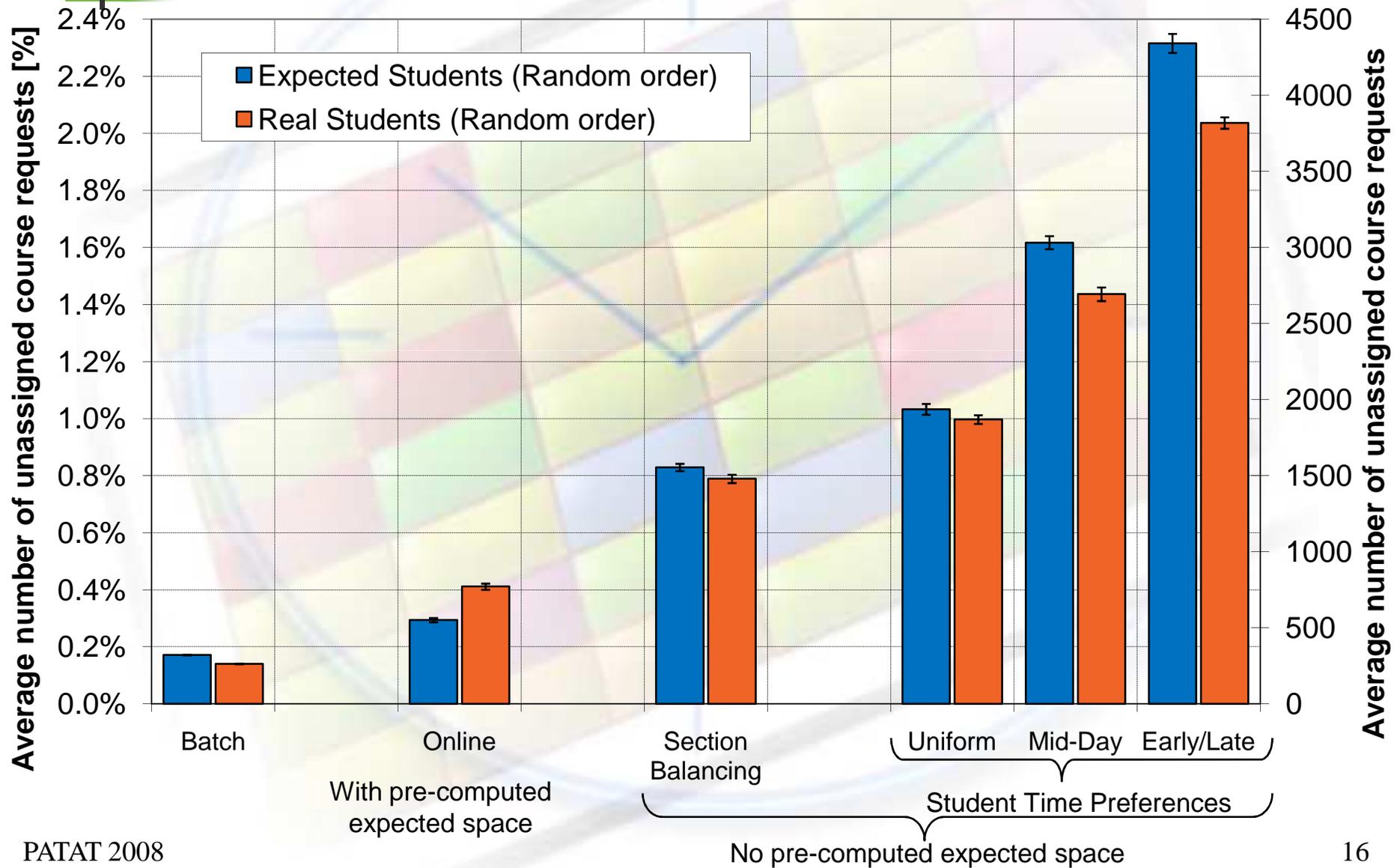
	Projected Students	Real Students
Batch Sectioning (Average \pm RMS of 20 runs)	0.171% \pm 0.001% (317.4 \pm 1.6)	0.140% \pm 0.001% (264.6 \pm 1.9)
Online Sectioning (Random order)	0.294% \pm 0.007% (545.2 \pm 13.5)	0.411% \pm 0.011% (772.5 \pm 20.3)
Online Sectioning (Students with more choices first)	0.401% \pm 0.007% (744.0 \pm 12.5)	0.556% \pm 0.008% (1043.7 \pm 15.0)
Online Sectioning (Students with less choices first)	0.249% \pm 0.002% (461.6 \pm 3.6)	0.318% \pm 0.002% (597.0 \pm 4.3)
Online Section Balancing (Random order, no expected space)	0.828% \pm 0.013% (1696.4 \pm 16.3)	0.789% \pm 0.015% (1481.9 \pm 27.4)

Practical Results: Batch versus Online

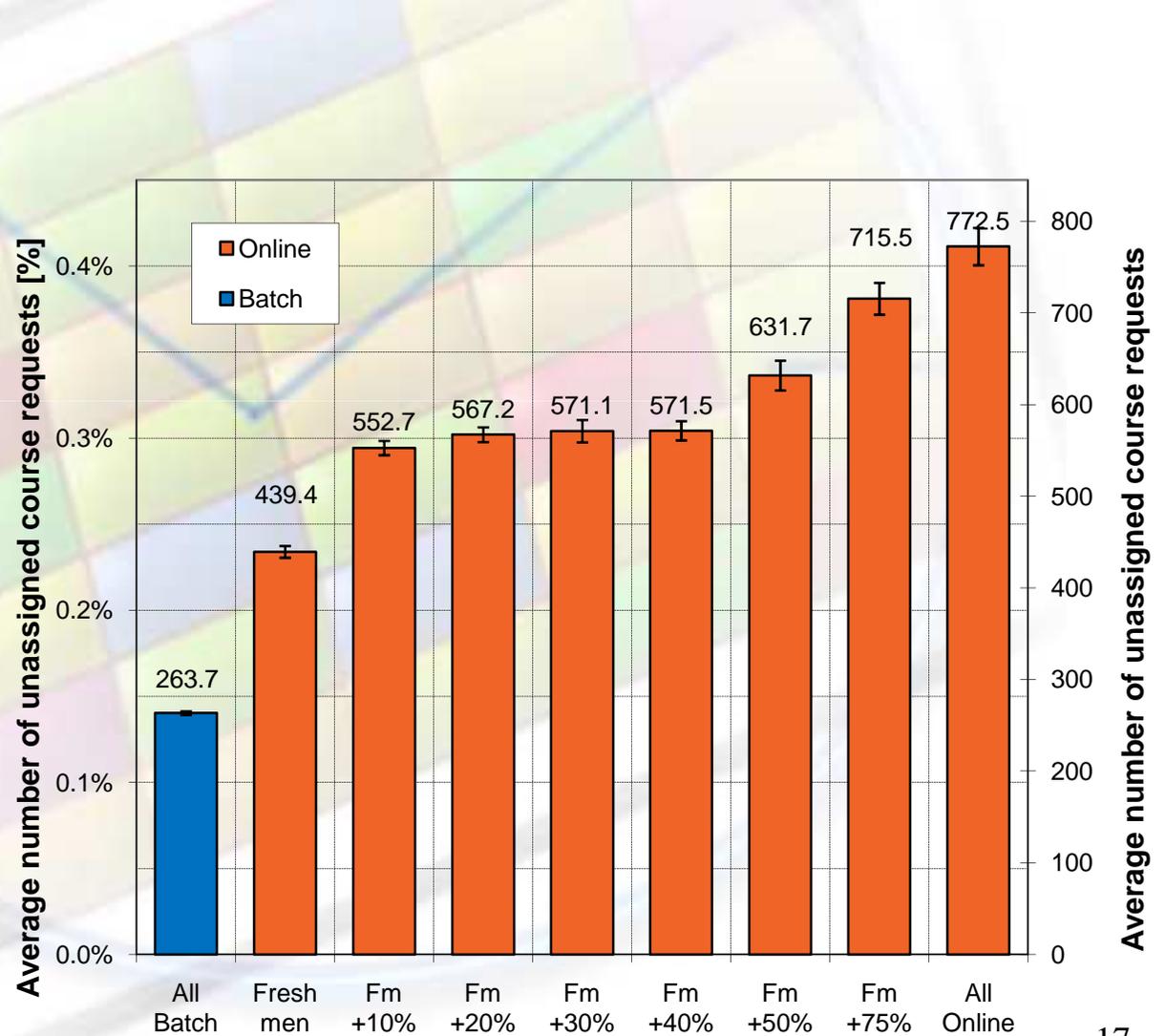
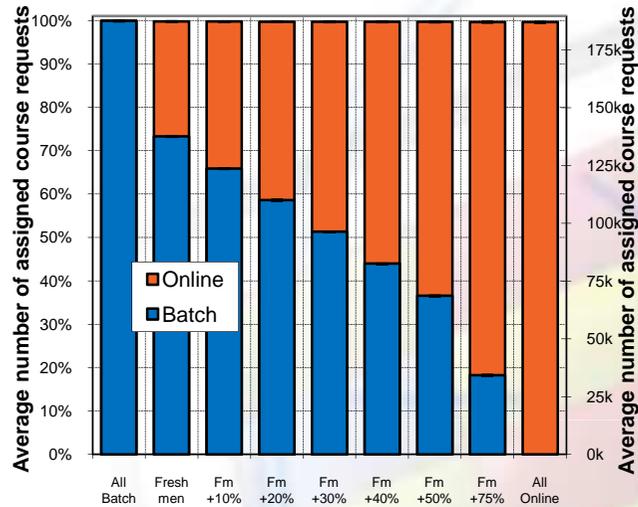
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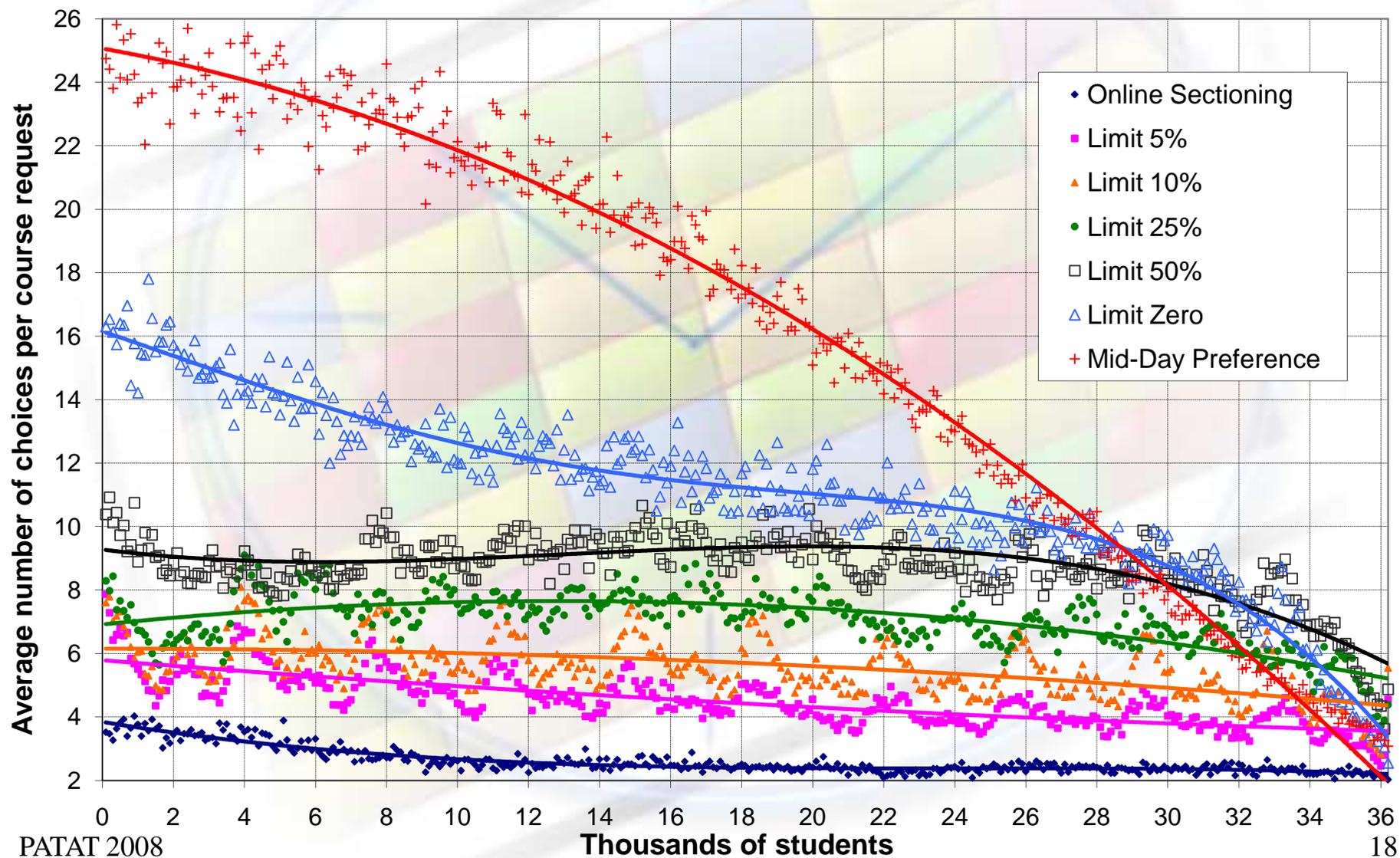
Practical Results: Batch, Online, Time Preferences



Practical Results: Combining Batch & Online



Practical Results: Student Choice

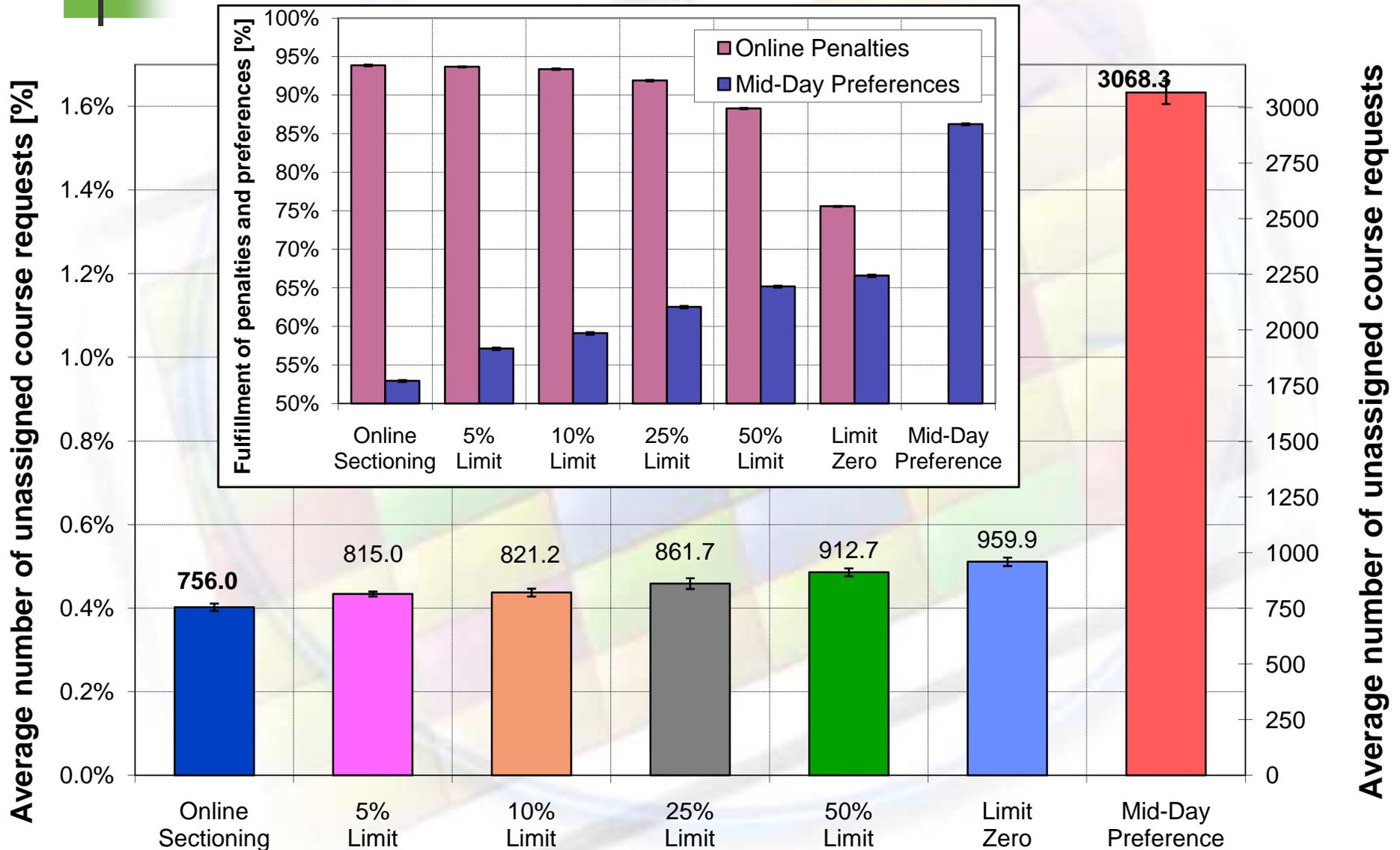


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Thousands of students

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Practical Results: Student Choice



Future Work

- Reservations
 - On courses or classes
 - Academic area, major / minor, learning-communities, individual
- Wait-listing on Courses
- Re-Sectioning
 - Wait-list processing, course timetable changes, mass cancellations, etc.
- Student Choices
 - (Limited) ability to choose time and instructor
 - Choice between available classes
 - Wait-listing for classes that are not available

1. ENGL 106

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Sel	Que	Time	Date	Instructor	Rec
<input checked="" type="radio"/>	<input type="checkbox"/>	Th 8:30a - 9:20a	Full Term		F 8:
 - ☑ Rec W 8:30a - 9:20a Full Term HEAV 225

Sel	Que	Time	Date	Instructor
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2. BIOL 110

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- ☑ Rec T 6:00p - 6:50p Full Term WTHR 360
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3. Free Time MWF 7:30a - 8:20a

Conclusions & Further References

■ Conclusions

- Demand based timetabling and sectioning provides the best results
 - However, master timetabling with online sectioning can be significantly improved using past information on student course demands
- The presented hybrid approach is highly applicable in practice
- Allows for earlier planning, but improves on the efficiency of current sectioning approaches

■ Further References

- <http://www.unitime.org>
 - Software available for download
 - Documentation
 - Ongoing research
 - Real-life benchmark data sets

